

TU4A-1

# Statistical Synthesis of Optimal Coupling Matrix for Robotic Automatic Tuning of Microwave Bandpass Filters

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  - A. Statistical Distribution of Coupling Elements
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- Deployment of 5G wireless communication systems
- Tuning of microwave filters
  - major factor in the production cost
- Enhancing the tuning efficiency in mass production
- Filter synthesis as a statistical problem
- Yield optimization<sup>[1]</sup>
  - requires good physical intuitive initial values

[1] J.W. Bandler and S.H. Chen, "Circuit optimization: the state of the art," IEEE Trans. Microwave Theory Tech., vol. 36, 1988, pp. 424-443.

- Mimicking the statistical tuning process of human
- Monte-Carlo optimization
- Statistically optimal Coupling Matrix (CM)
  - viable physical design
  - efficient tuning process in mass production
- Infinite number of CMs that meets a given specification
- CM with equi-ripple return loss (RL) <sup>[2]</sup>
  - more vulnerable to the tuning error

[2] R. J. Cameron, C. M. Kudsia, and R. R. Mansour, Microwave Filters for Communication Systems. New York: Wiley, 2007, ch. 6–8.

- **Robotic automatic tuning (RAT)**
  - filter model extraction techniques [3]-[5]
  - mechanic error
  - extracted CM and target CM<sup>[6]</sup>
- **Statistically optimal Coupling Matrix**
  - center of “Disneyland”

[3] P. Harscher, R. Vahldieck and S. Amari, "Automated filter tuning using generalized low-pass prototype networks and gradient-based parameter extraction," IEEE Trans. Microw. Theory Techn., vol. 49, no. 12, pp.2532-2538, Dec. 2001.

[4] G. Macchiarella and M. Santoniccolo, "An Original Technique for Computer-Aided Tuning of Microwave Filters," 31st Eur. Microw. Conf., 2001, pp. 1-4.

[5] M. Meng and K.-L. Wu, "An analytical approach to computer-aided diagnosis and tuning of lossy microwave coupled resonator filters," IEEE Trans. Microw. Theory Techn., vol. 57, no. 12, pp. 3188–3195, Dec. 2009.

[6] P. Zhao, K.-L. Wu, "Model-Based Vector-Fitting Method for Circuit Model Extraction of Coupled-Resonator Diplexers", IEEE Trans. Microw. Theory Techn., vol. 64, no. 6, pp. 1787-1797, June 2016.

# Statistical Distribution of Coupling Elements

- **Statistical Distribution**
  - collect as many CMs as possible
  - just satisfies the given specification
- **Non-linear optimization**
  - emulates the human tuning process
  - just meets the tuning/design specification
  - tuning specification vs. acceptance specification

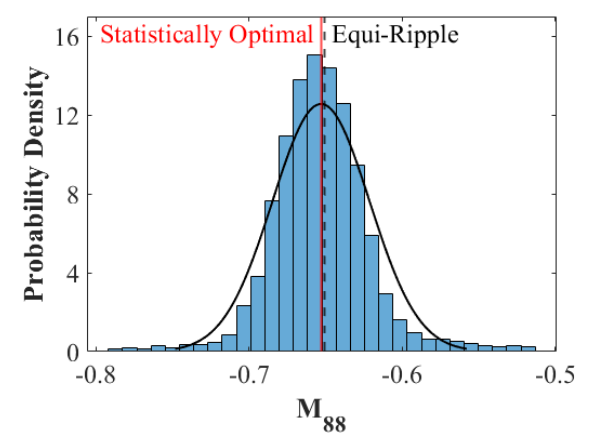
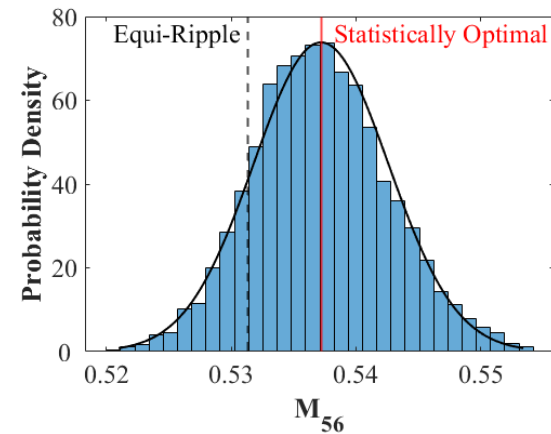
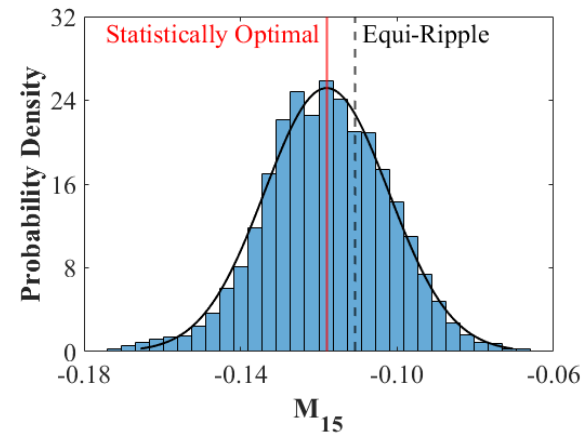
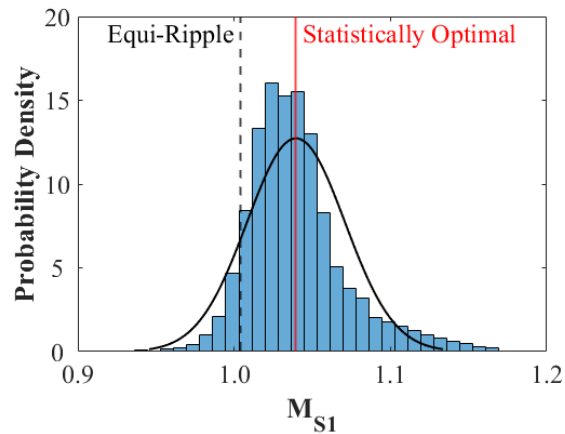
# Statistical Distribution of Coupling Elements

- Monte-Carlo optimization

–solve:  $\min_x \max_i F_i(g(x))$

$g(x)$  : insertion and return loss

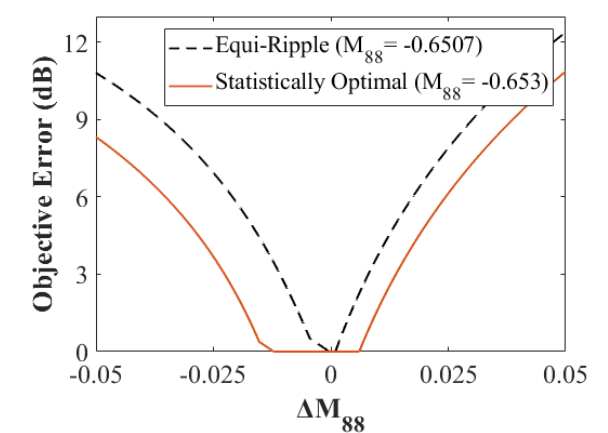
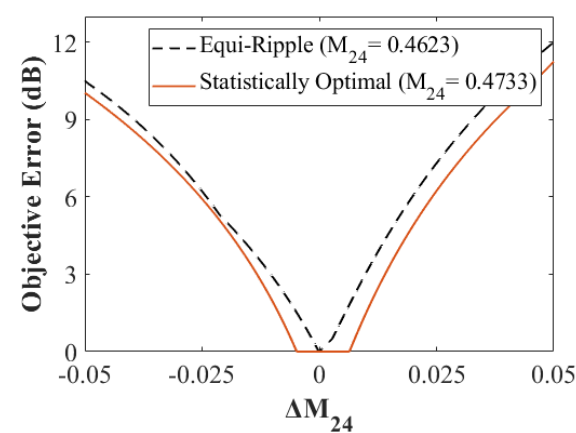
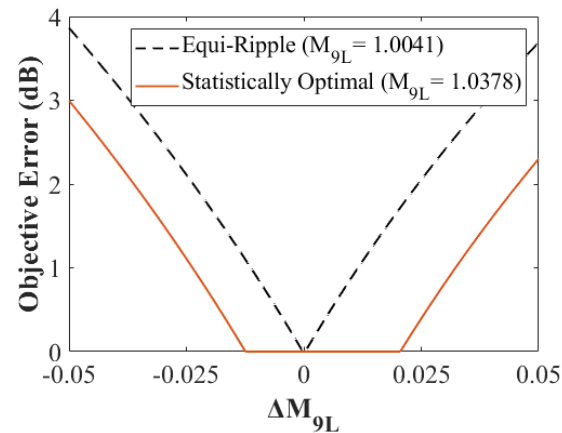
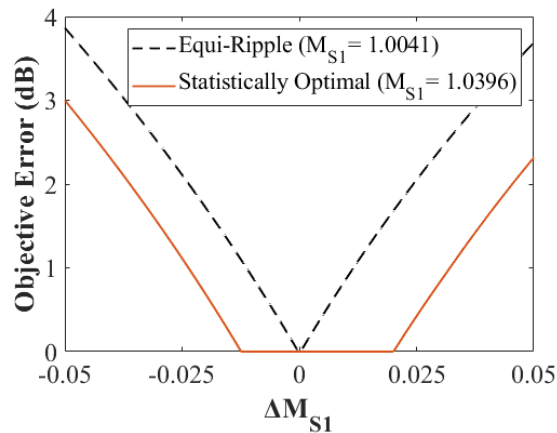
$F(\cdot)$  : objective function



- Sensitivity analysis of each coupling element

$$-Err = \max_i \max(g(x) - z, 0)$$

$z$  : design specification



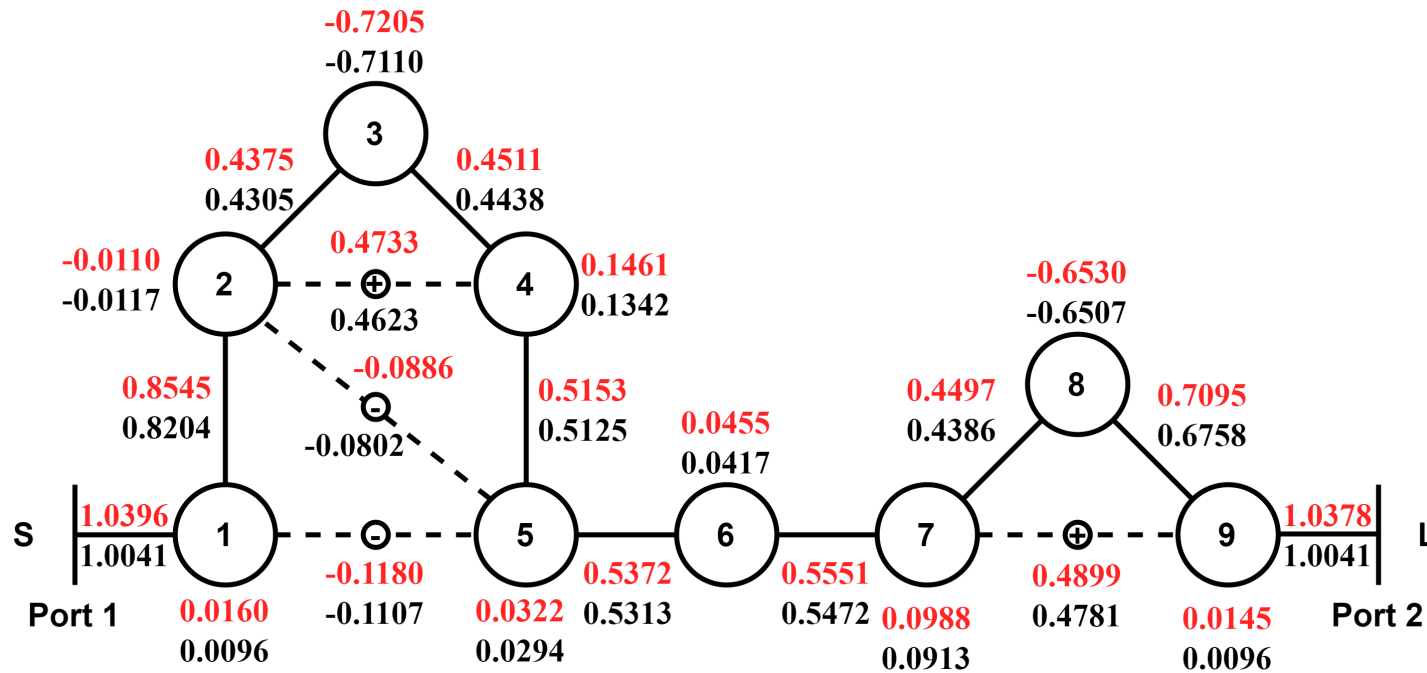


# Monte-Carlo Analysis

- Overall sensitivity analysis of a given CM
- Tolerance analysis of microwave filters
- Uniformly distributed random variables
- Estimated yield
  - acceptance specification

# Verification Example

- 9th-degree filter with 4 transmission zeros (TZs)

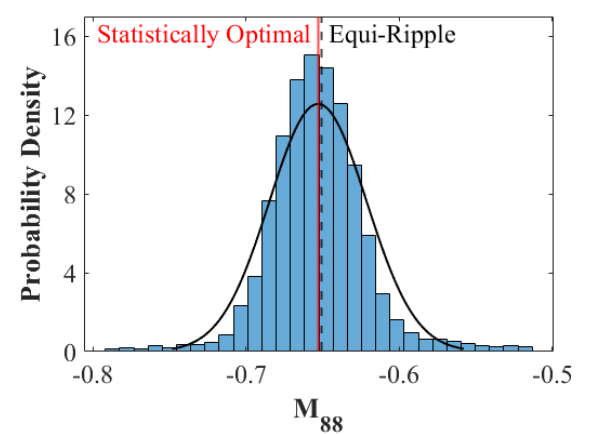
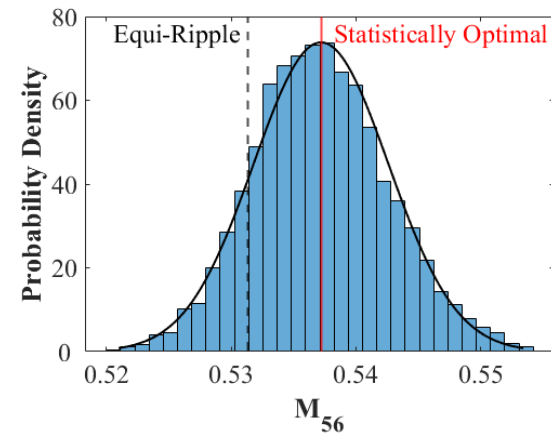
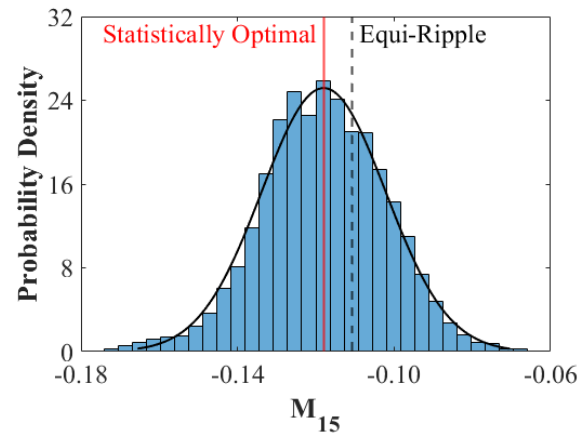
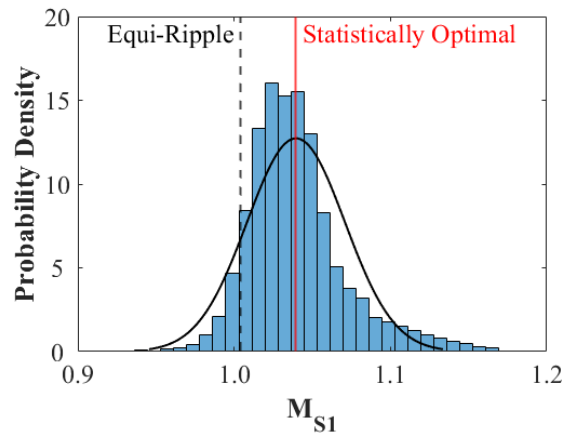


Red: Statistically Optimal CM

Black: Equi-Ripple CM

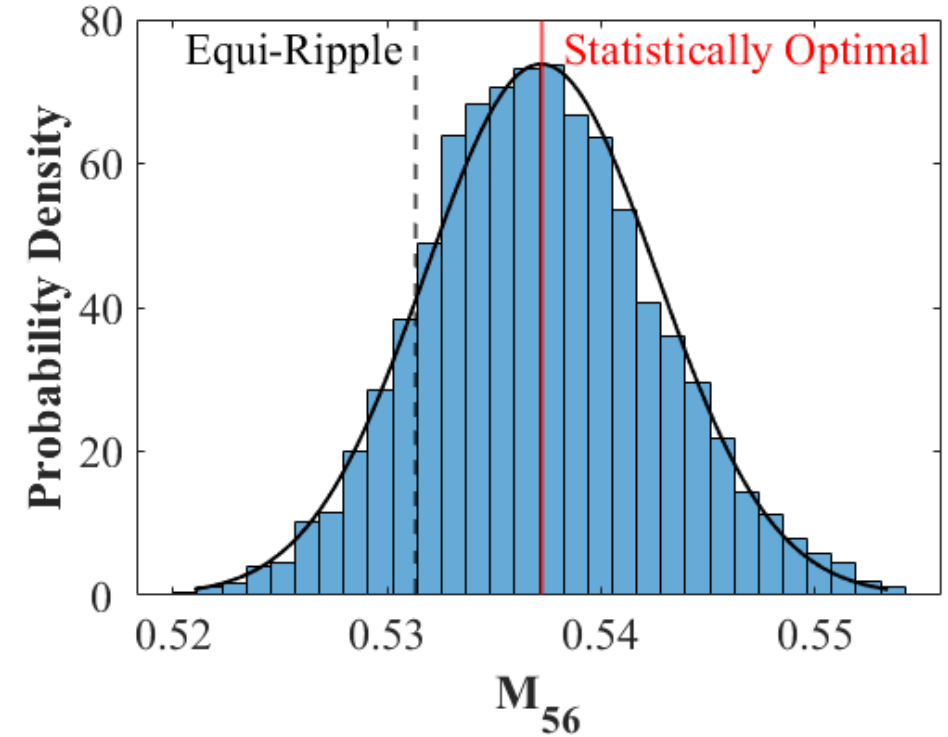
# Verification Example

- Statistical Distribution
  - 5000 optimized samples
  - $\pm 0.05$  of the initial values (uniform distribution)
  - normal distribution



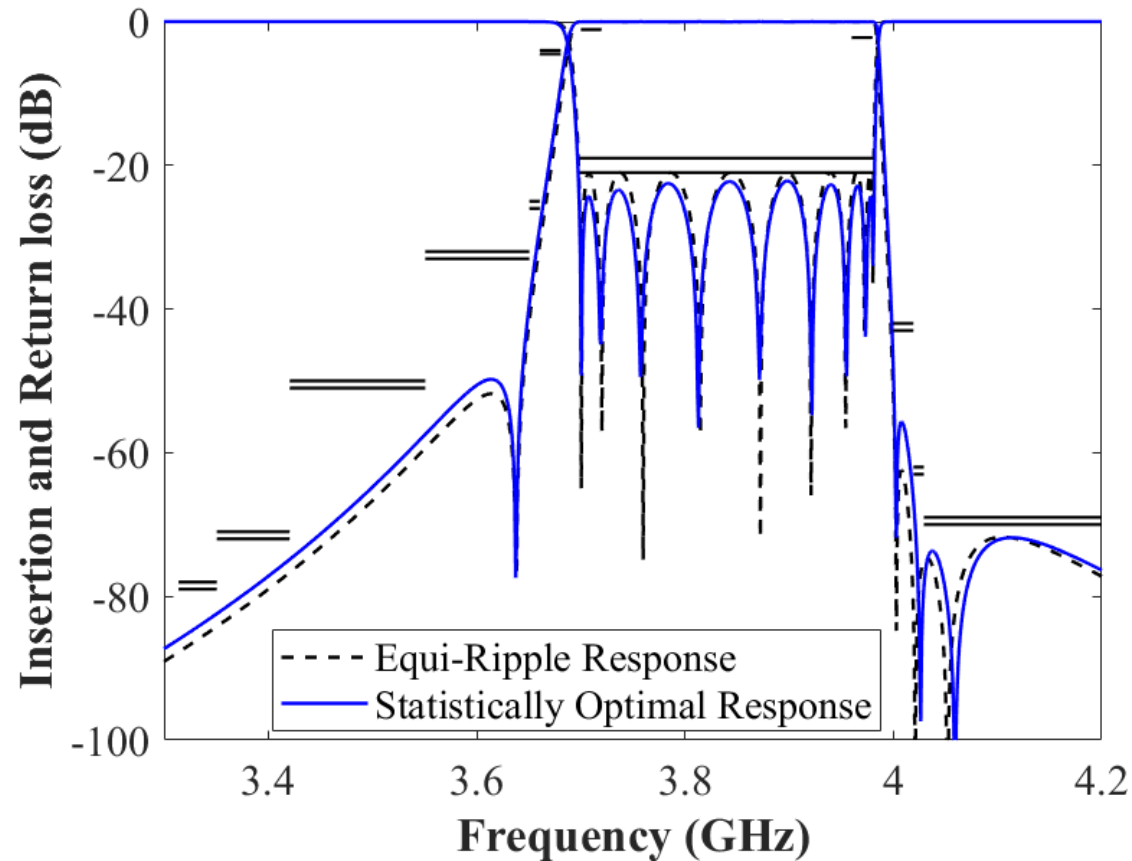
# Verification Example

- **Statistically Optimal CM**
  - optimal value (mean)
  - highest probability density
- **Equi-Ripple CM**
  - far away from the optimal
  - not optimal for the ease of tuning

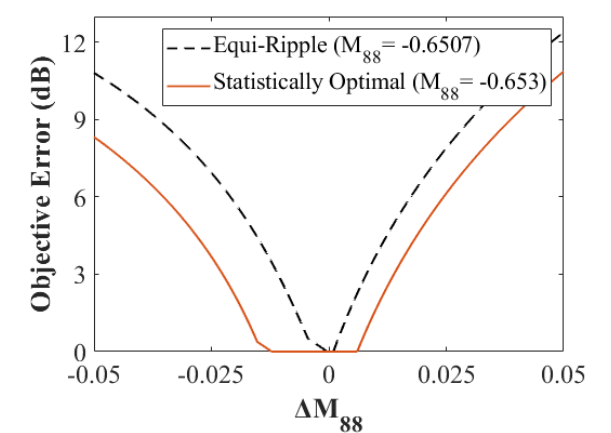
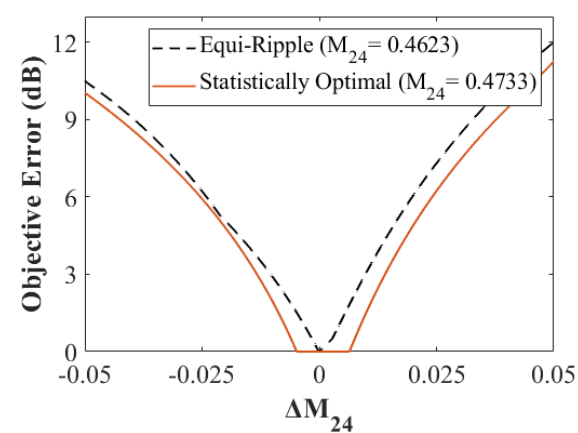
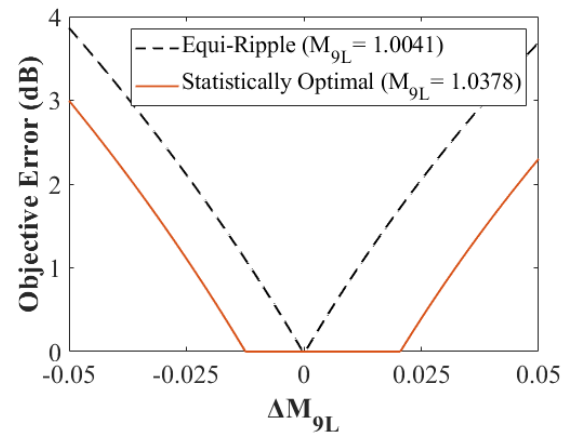
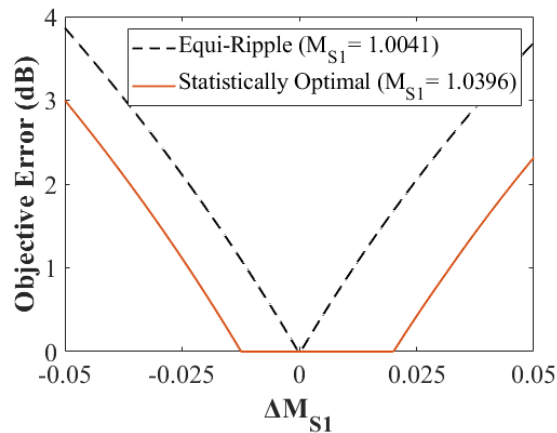


# Verification Example

- Equi-Ripple response vs. Optimal response

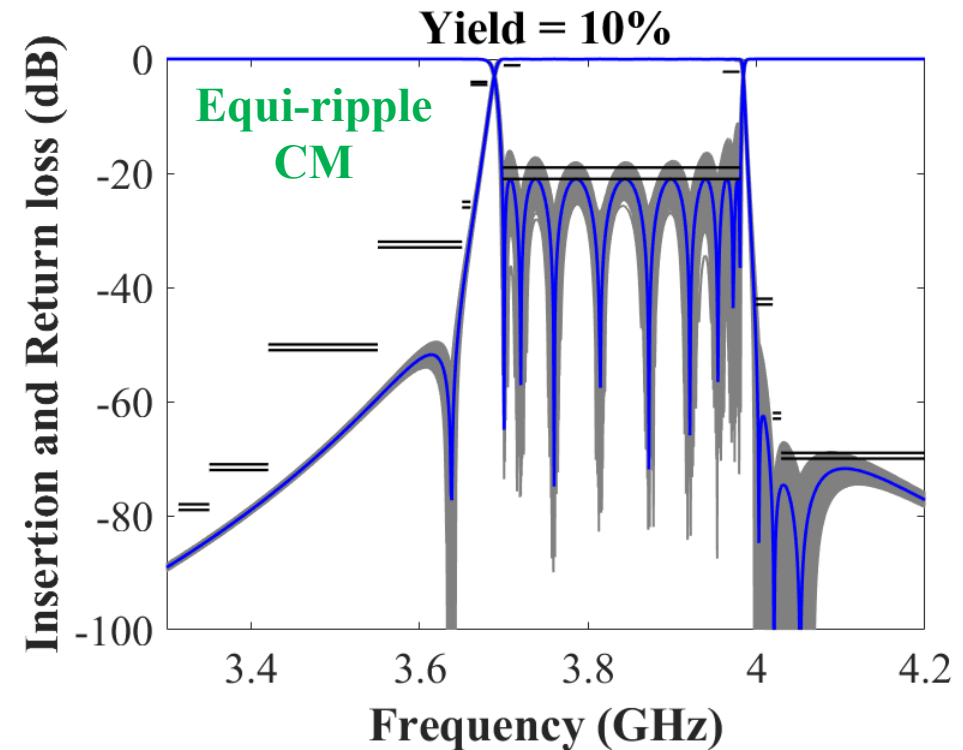
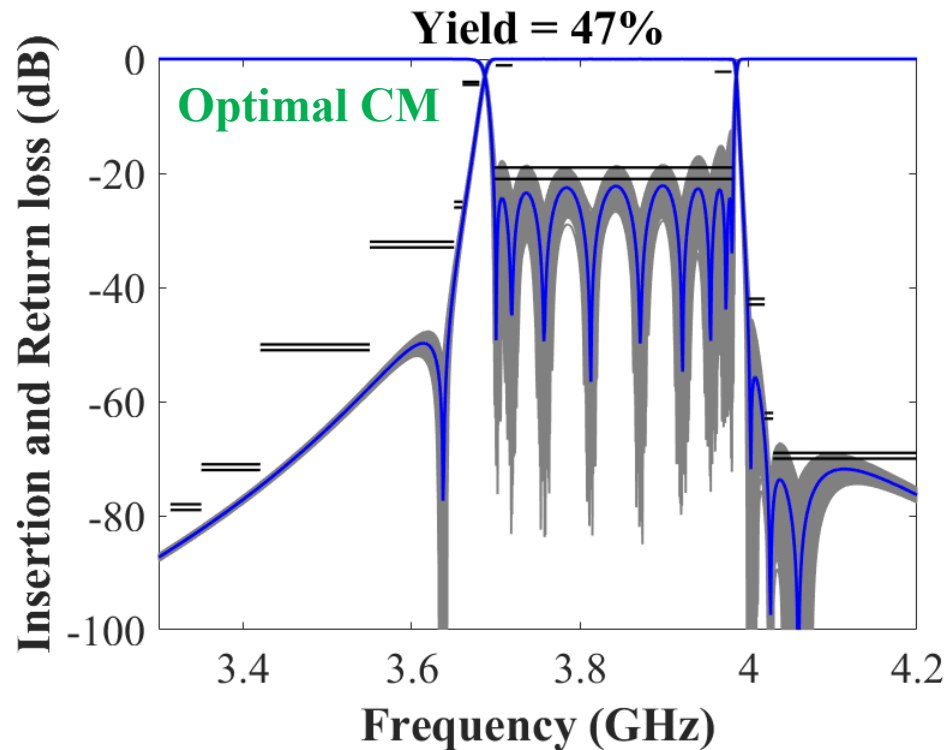


- V-curves
  - zero-error regions
  - relatively gradual slope



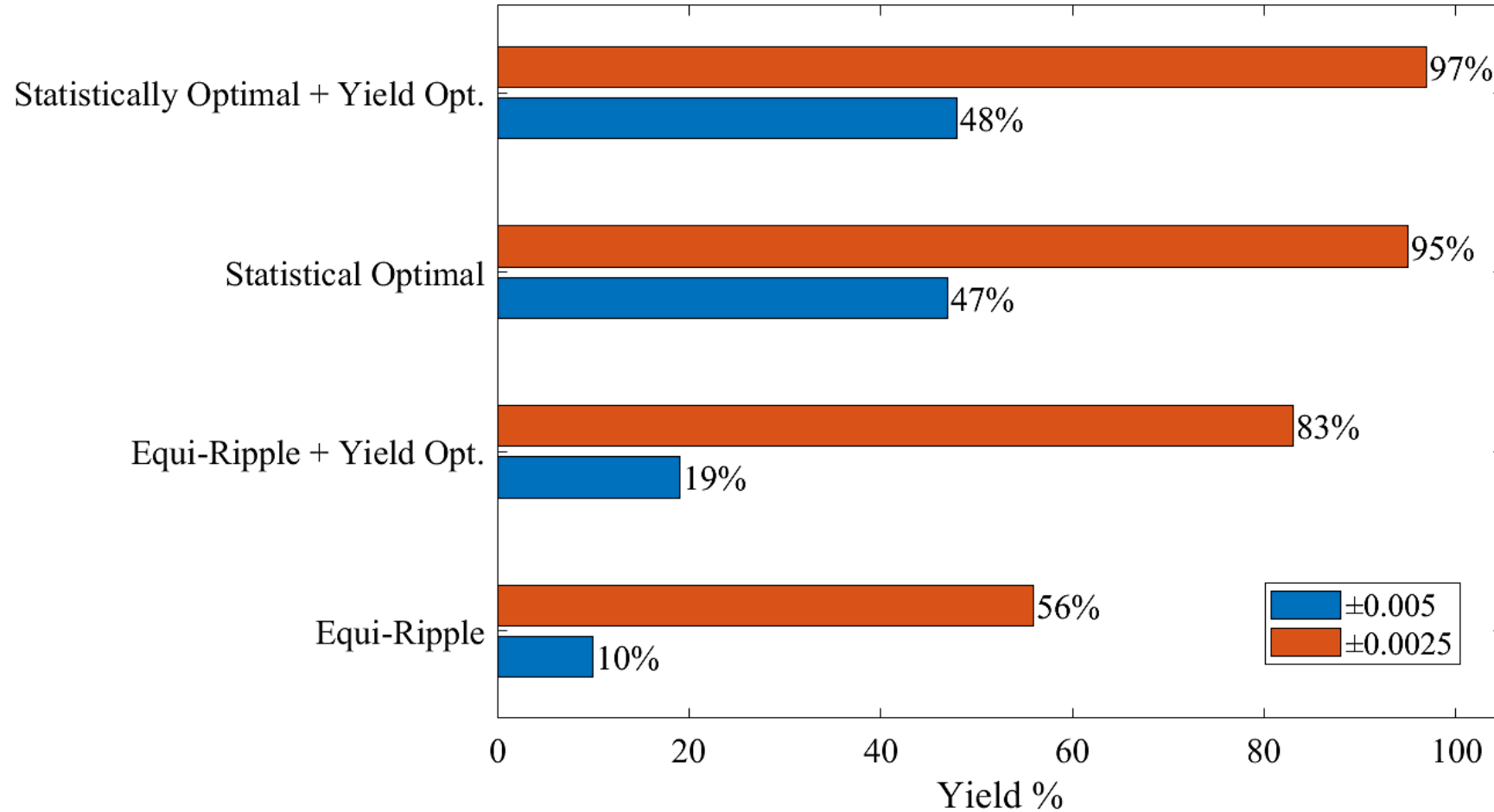
# Verification Example

- Monte-Carlo simulation  
– 10,000 samples,  $\pm 0.005$



# Verification Example

- Monte-Carlo simulation





# Conclusion

- **Equi-ripple CM is not statistically optimal**
- **V-curves and Monte-Carlo analysis give further evidence**
- **Superiority of the statistically synthesized optimal CM**