



#### **TU4A-4**

# Analysis of a Sensor Based on an Injection-Locked Oscillator Driven by a Chirp Signal

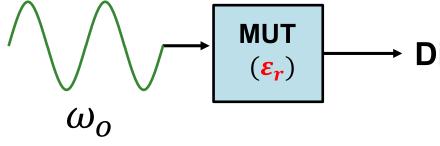
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#### Material under test (MUT):



**Analysis frequency** 

## Dielectric constant at $\omega_o$ :

$$\frac{\varepsilon_r}{\varepsilon_r} = \varepsilon' + j\varepsilon'' = \frac{\varepsilon'}{\varepsilon'} (1 + \tan \delta)$$

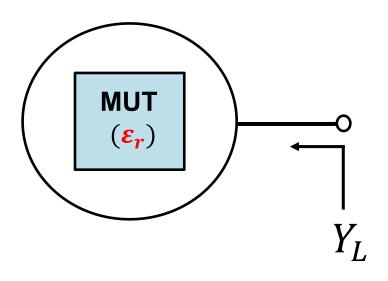
Parameters to be detected

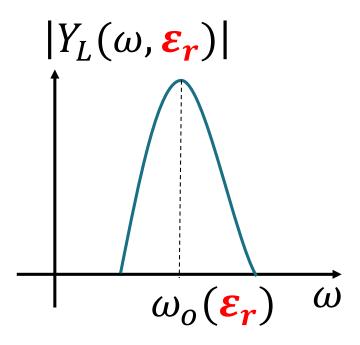






#### Resonator: linear circuit



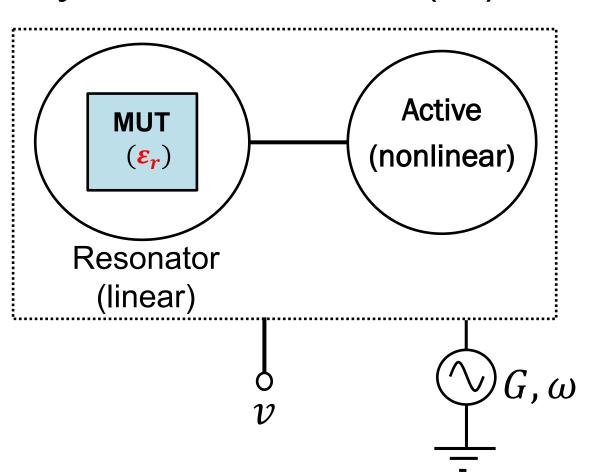








#### Injection locked oscillator (ILO) sensor:



$$v(t) = \sum_{k} V_k(t)e^{j(k\omega t + \phi_k(t))}$$

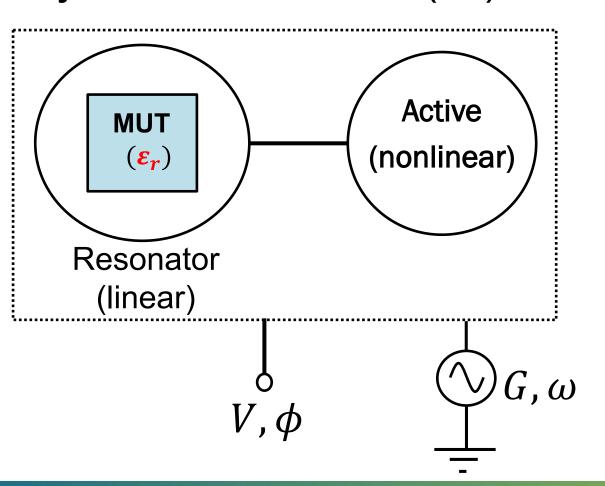
$$V = V_1(t, \boldsymbol{\varepsilon_r}) \longrightarrow$$
 Observation variable

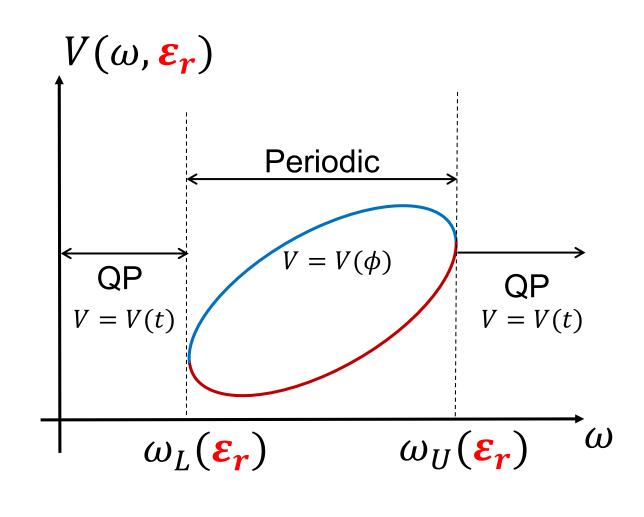






#### Injection locked oscillator (ILO) sensor:



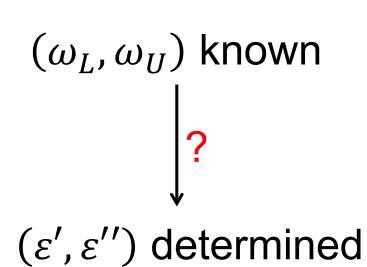


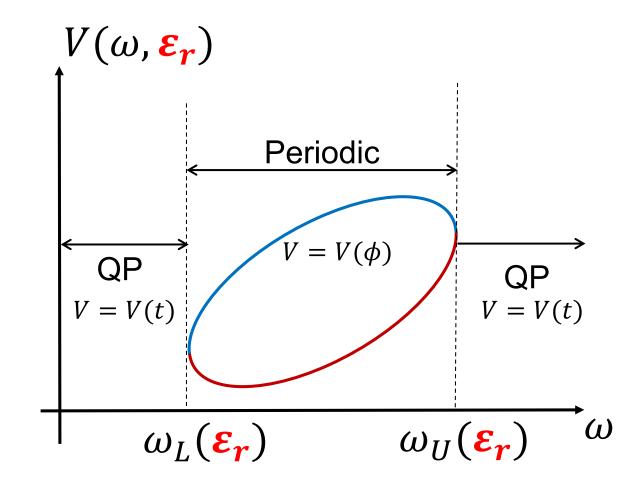






#### **Estimation:**



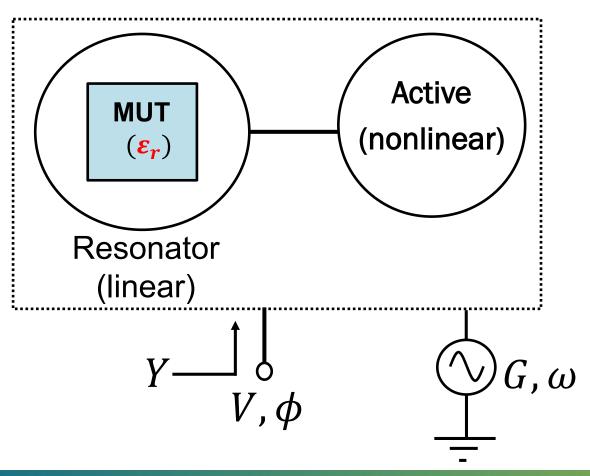


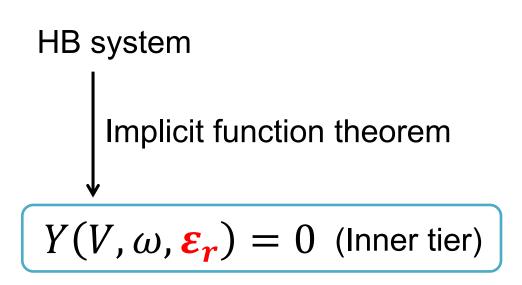






#### System equations:



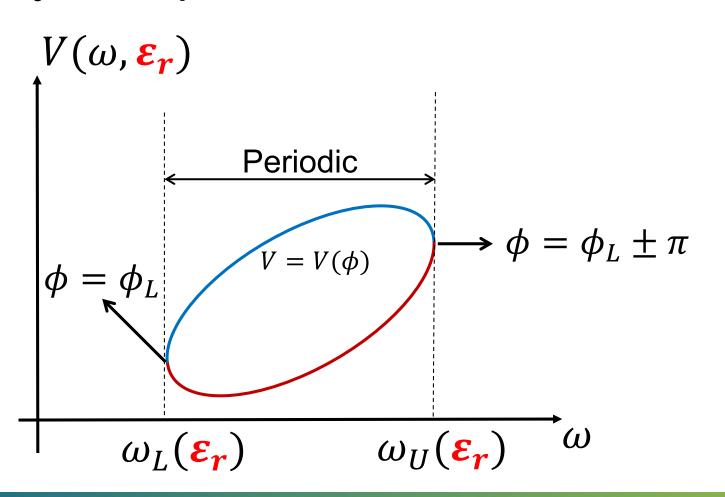








#### System equations:



#### Border conditions:

$$\frac{\partial \omega}{\partial \alpha} = 0$$

$$\omega(\phi) - \omega_U = 0$$

$$\omega(\phi \pm \pi) - \omega_L = 0$$







System equations:  $u = \{V, \omega, \phi, \varepsilon', \varepsilon''\}$ 

$$Y(V, \omega, \boldsymbol{\varepsilon_r}) = 0$$

$$\frac{\partial \omega}{\partial \alpha} = 0$$

$$\omega(\phi) - \omega_{II} = 0$$

$$\omega(\phi \pm \pi) - \omega_L = 0$$

$$F(u, \omega_L, \omega_U) = 0$$

$$\omega(\phi) - \omega_U = 0$$

$$\omega(\phi \pm \pi) - \omega_L = 0$$

$$(\varepsilon', \varepsilon'') = f(\omega_L, \omega_U) \Leftrightarrow \det \frac{\partial F(u, \omega_L, \omega_U)}{\partial u} \neq 0$$

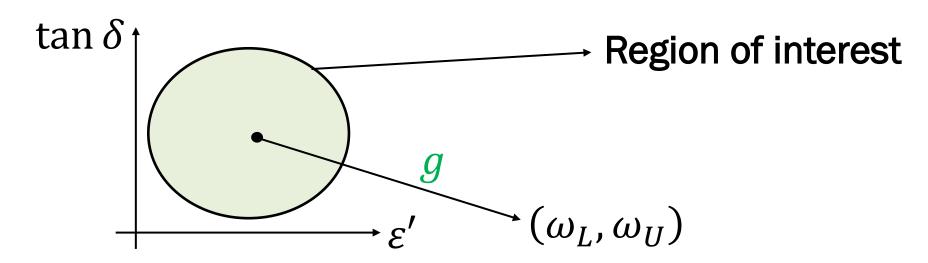






Calibration of the Sensing function:  $(\varepsilon', \tan \delta) = f(\omega_L, \omega_U)$ 

1) Detection of  $(\omega_L, \omega_U) = g(\varepsilon', \tan \delta)$ 



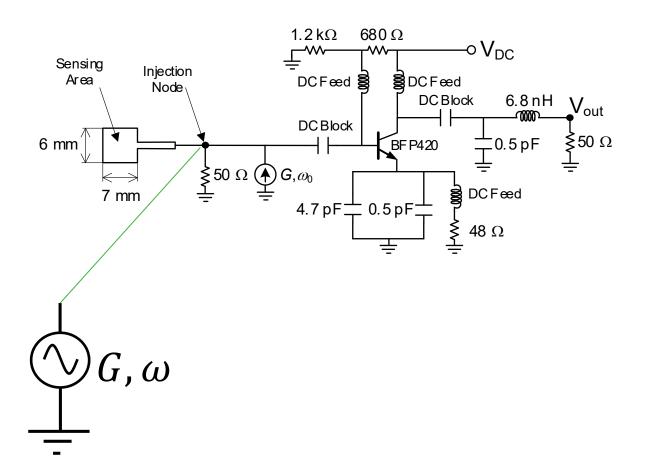
2) Obtain  $f = g^{-1}$ 



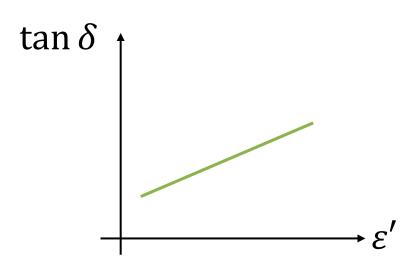




#### Injection-locked oscillator based on the NPN bipolar transistor BFP420



## Region of interest:



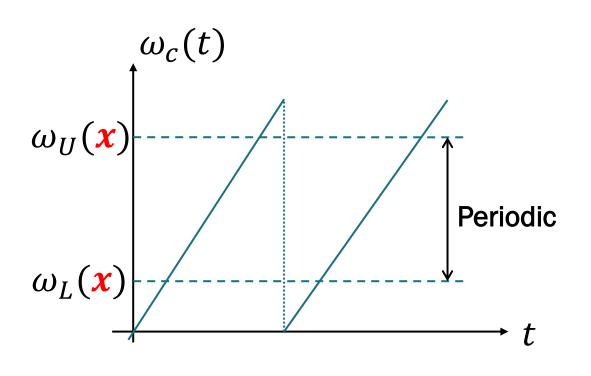
$$\varepsilon' = 1 + x$$
$$\tan \delta = 0.002 + 0.001x$$

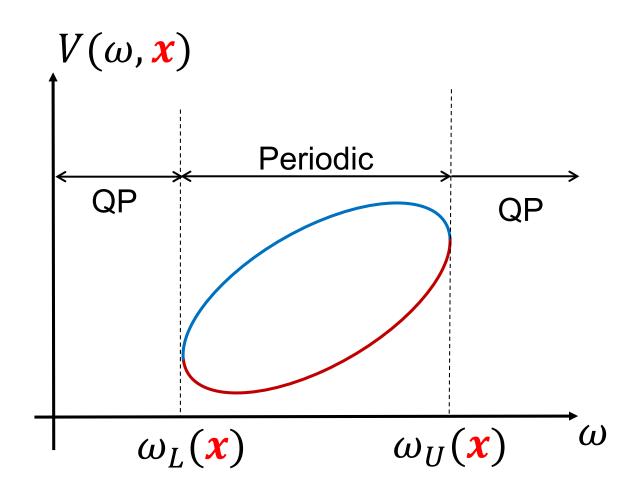






## Injection source: chirp signal







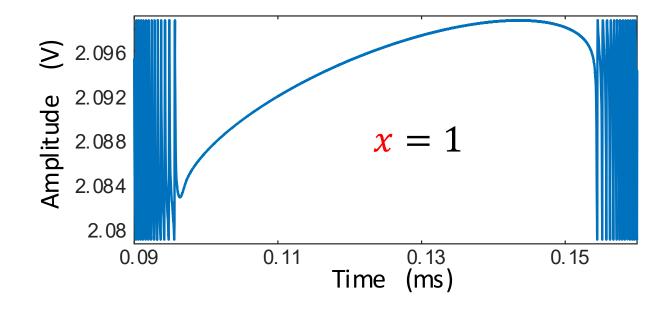




## Injection source: chirp signal

Inner tier:  $Y(V, \omega, \mathbf{x}) = 0$ 

$$Y_V(V - V_o) + Y_\omega \left(\omega_c - \omega_o + \dot{\phi} - j\frac{\dot{V}}{V}\right) + GY_g(\phi) = 0$$

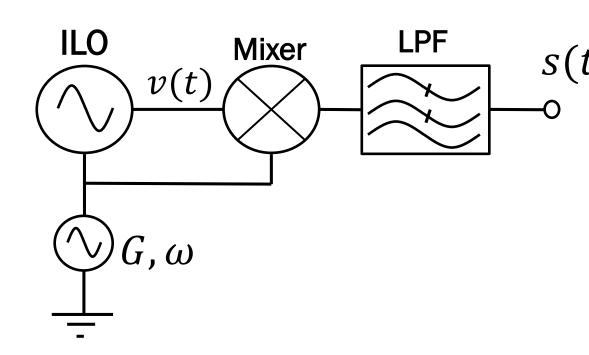




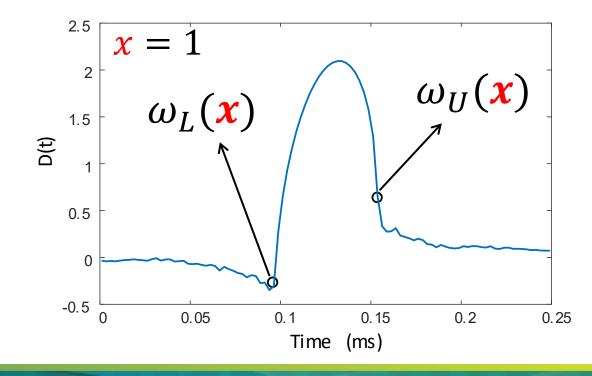




## Detection of $\omega_L$ and $\omega_U$



## Averaging:

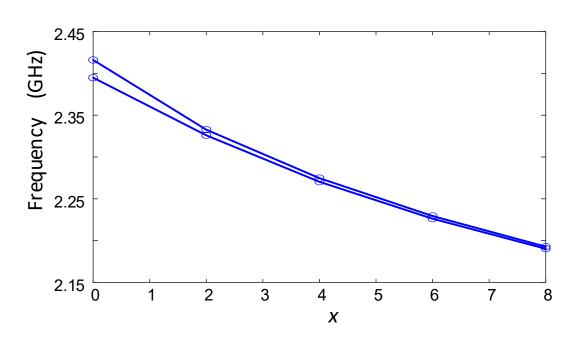




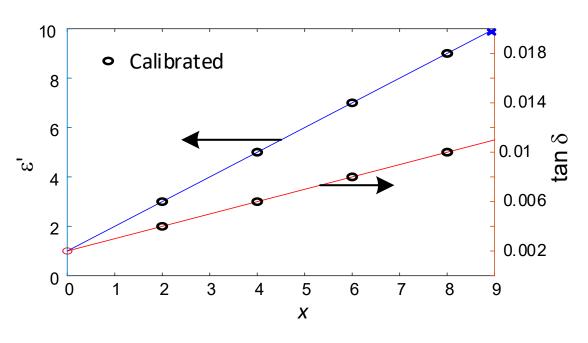




#### **Calibration:**



$$(\omega_L(\mathbf{x}), \omega_U(\mathbf{x})) = g(\varepsilon'(\mathbf{x}), \tan \delta(\mathbf{x}))$$



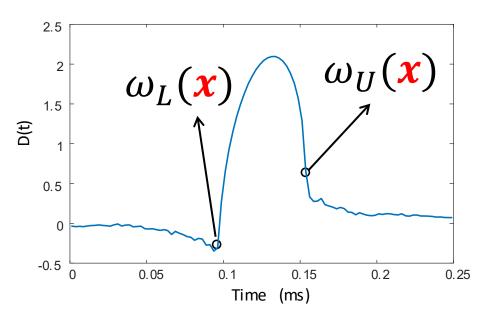
$$(\varepsilon'(\mathbf{x}), \tan \delta(\mathbf{x})) = f(\omega_L(\mathbf{x}), \omega_U(\mathbf{x}))$$

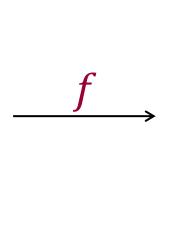


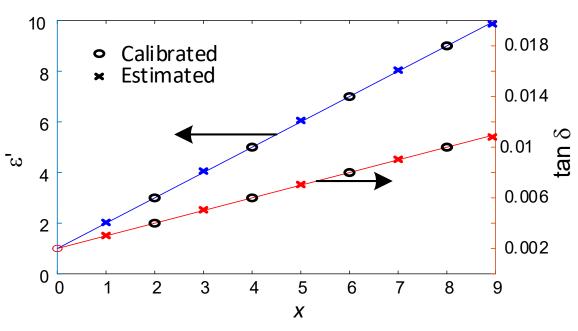




#### **Estimation:**







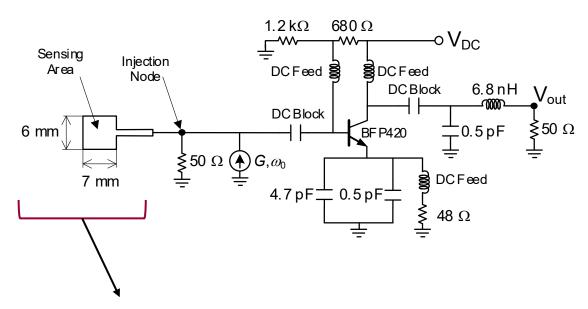




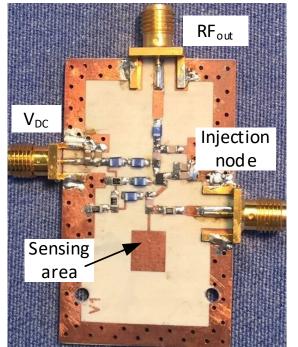
## **Application**

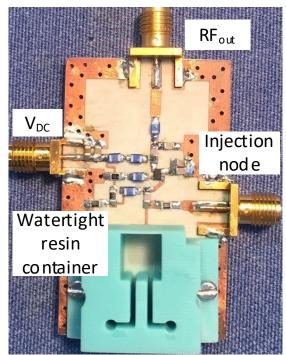


#### x: Concentration of ethanol in water



Capacitive section of the resonator





Prototype built on Rogers 4003C substrate with and without the resin container

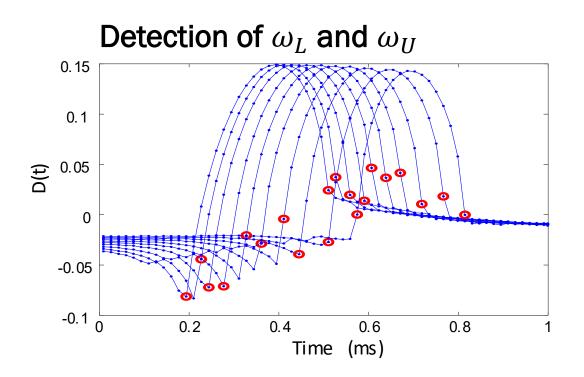




# **Application**



#### x: Concentration of ethanol in water



#### **Estimation of** $\varepsilon'$ **and** tan $\delta$ Calibrated **×** Estimated 60 0.8 -ယ 40 0.6 20 0.4 0.2 20 30 80 40 50 60 70 90 10 Percentage (%)





# Summary



- Sensor based on an injection-locked oscillator driven by a chirp signal
- The time interval for which the oscillator gets locked to the injection source depends on the MUT
- This time interval can be detected and used to estimate the MUT

