



Comparison of Analytical Solutions and Numerical Optimization in Beamforming

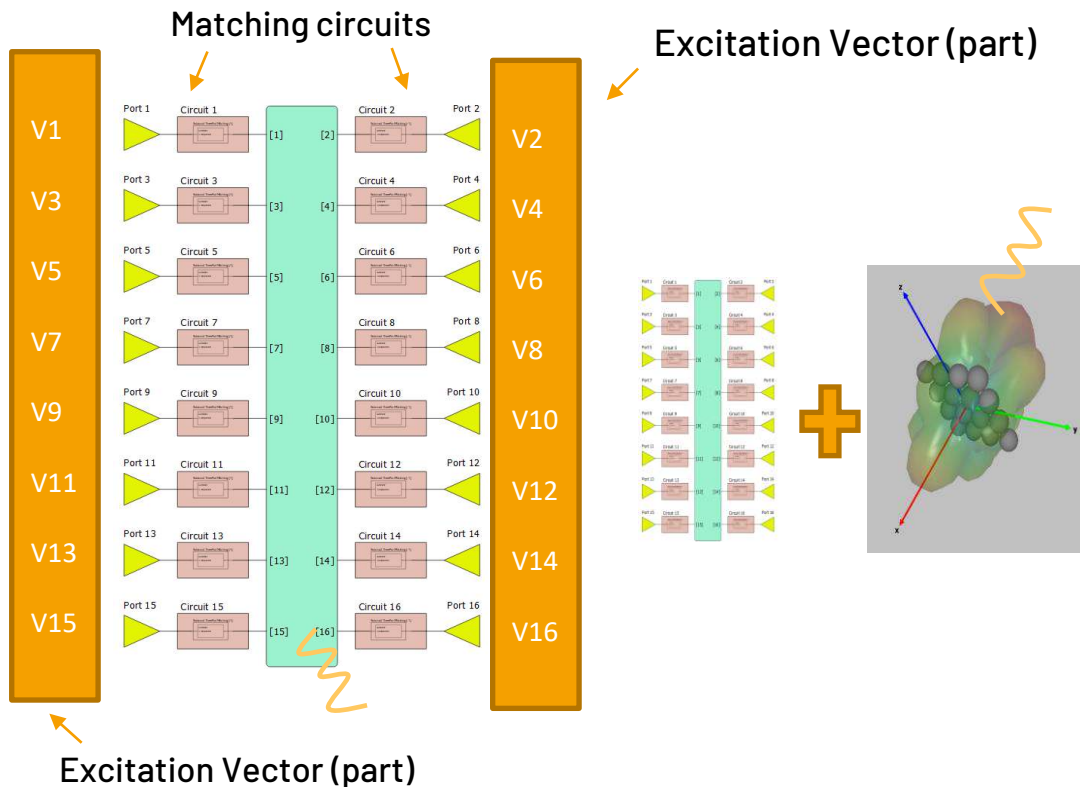
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Outline of this Presentation

- General Array Feeding Challenge
- Array factor vs. Full Array analysis
- Canonical (Analytical) solutions for array excitation in Optenni Lab
 - Progressive phase shift
 - Plane wave excitation
 - Maximal gain
 - Amplitude tapering schemes
- Numerical optimization in Optenni Lab
 - Breaking free from canonical excitation schemes
- Comparison of canonical and numerical solutions in terms of **EIRP**

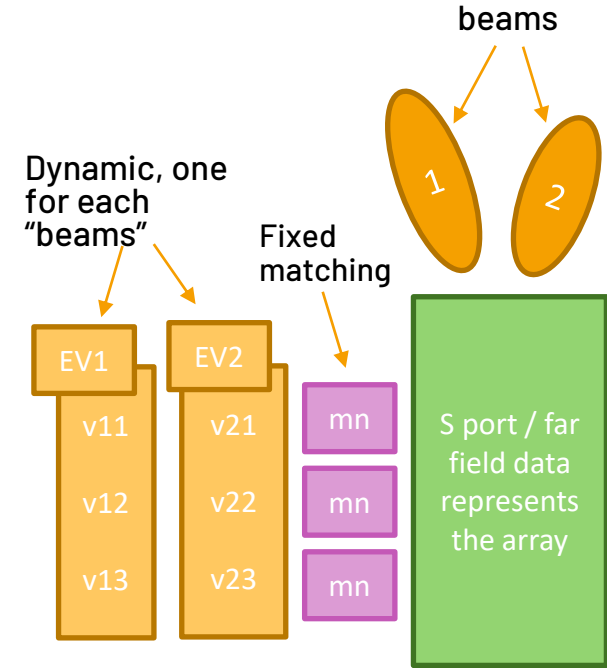
General Array Feeding Challenge

- Assuming a given physical array element structure...
- challenge is to find **excitation vectors (EV) + feeding & matching circuits**
- EVs create the wanted radiation characteristics but also alter the matching
- Power is coupled from other ports at the same frequency → active reflection coefficients, ARCs



So the Challenge Is To Determine...

- ...EVs that create the required radiation characteristics
 - Beams / EIRP
 - Sidelobe levels
 - Nulls
 - Polarization etc etc
- ... so that the matching due to ARCs is acceptable, and
- ... and so that the power output/dynamic range of the amplifiers generating the EVs is reasonable
- A complexity management challenge!
- **Optenni Lab makes it a breeze!**



Two Approaches: Array Factor vs. Full Array Analysis

- Array factor analysis
 - Radiation is a multiple of single element and array factors
 - The radiation pattern of a single antenna element is used
 - The pattern is replicated to other elements in the array grid
 - The S parameters and coupling between the elements are ignored
- Full array analysis
 - All the radiation patterns of the array are used
 - The full S parameter matrix is used, including coupling terms
 - For any excitation, matching and termination condition the performance of the array is calculated exactly in Optenni Lab (no new EM simulation needed)
 - In this presentation, all results are from Optenni Lab & based on **full array** analysis

Canonical solutions in Optenni Lab

- Excitations with progressive phase shift between the elements (in two dimensions)
 - EVs phased at fixed intervals
- Excitation from a plane wave from a given direction
 - Theoretical phases of an ideal plane wave at the element locations
- Maximal available gain to a given direction
 - Can be computed with closed-form equations
- Amplitude tapering schemes to reduce side lobes
 - Binomial minimizes the sidelobes but creates highly uneven power distribution over EVs
 - Dolph-Chebyshev creates sidelobes of equal height

Enter canonical solution data

☒ Use progressive phase shift
☐ Use plane wave direction
☐ Use maximal available gain

Grid1: -Y

Progressive phase shift (degrees) 0

Amplitude tapering

☐ Uniform
☐ Binomial
☒ Dolph-Chebyshev

Sidelobe level -20

Grid2: +Z

Progressive phase shift (degrees) 0

Amplitude tapering

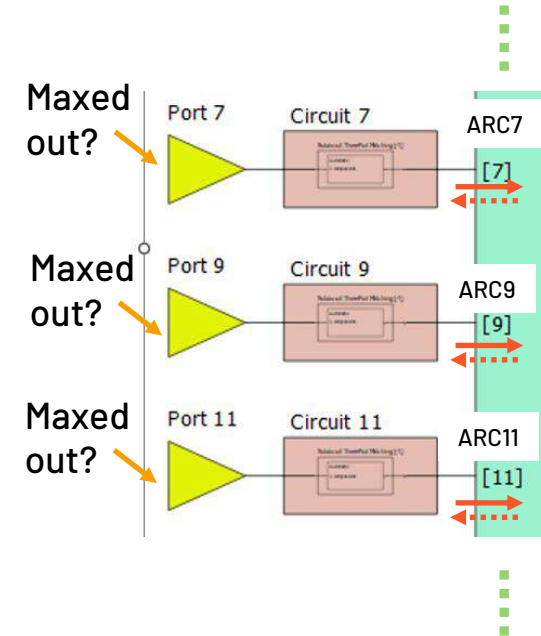
☐ Uniform
☐ Binomial
☒ Dolph-Chebyshev

Sidelobe level -20

OK Cancel Help

EIRP Of An Array – An Elusive Concept

- EIRP (effective isotropic radiated power)
 - hypothetical power that would have to be radiated by an isotropic antenna to give the same signal strength as the antenna in a given direction
- $EIRP = Gain(\theta, \phi) * IncidentPower$
- But, remember that for arrays,
 - IncidentPower is a **sum** of incident powers at the array's ports
 - Amplifiers of ports have a maximum power that **limit the dynamics** of the **tapering**
 - Active reflection coefficients → **how much power really gets radiated?**

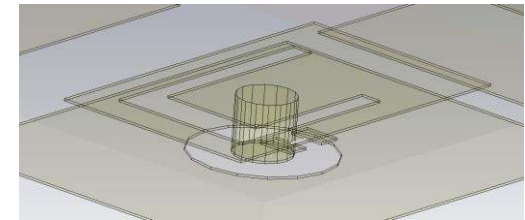
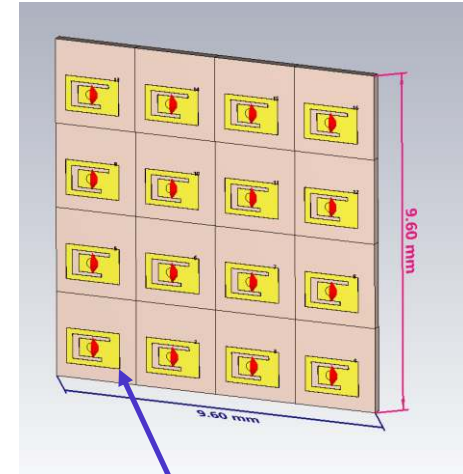
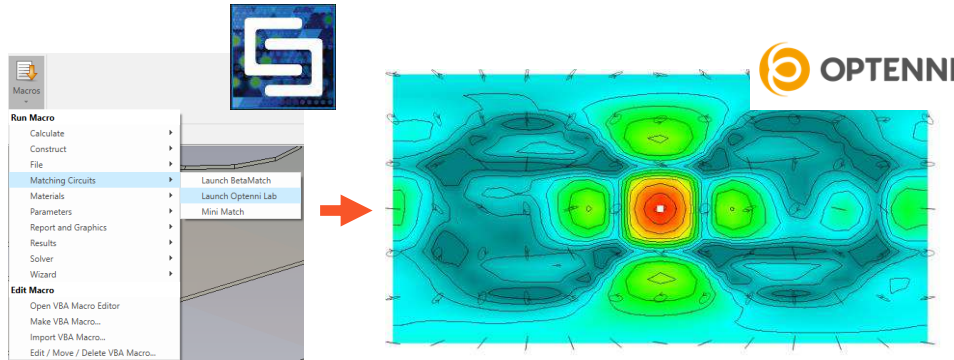


EIRP Of An Array – An Elusive Concept (continued)

- Expected the effects of the amplitude tapering are:
 - Side lobe levels are reduced
 - Realized gain is reduced
 - EIRP can be dramatically reduced
- **Optenni Lab makes this complexity a lot more manageable**

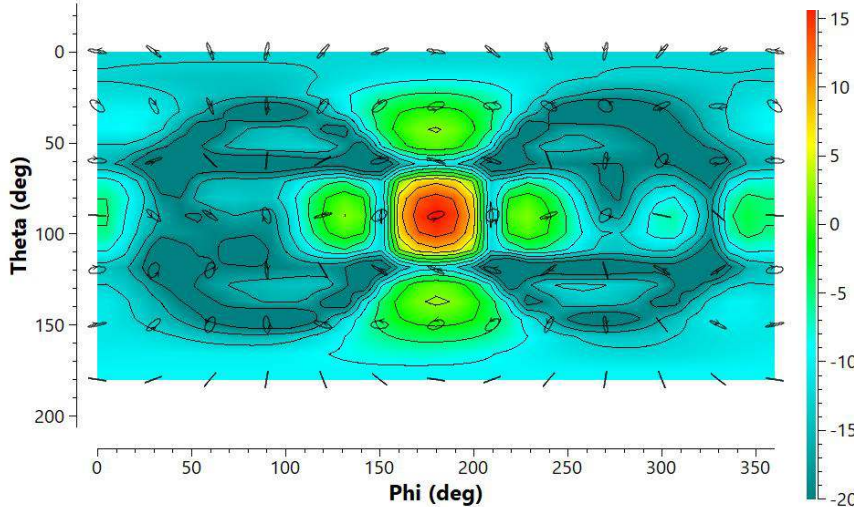
Example – A Compact mm Wave 4x4 Array

- Let's analyze the 16 port structure in 3D EM (here, Dassault/CST MWS)
 - Compute radiation patterns and 4x4 S parameter system
 - Push the results to Optenni Lab from CST's **Home > Macros > Optenni Lab**



Two Canonical Solutions for the 4x4 Array

Both figures have uniform excitation (broadside beam) at 60.25 GHz

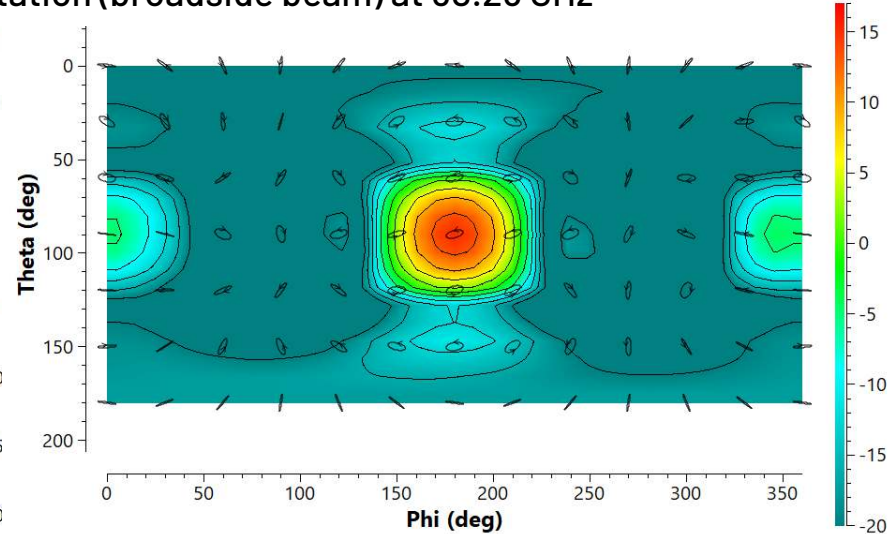


No tapering

Max gain 16.4 dBi

Max EIRP 58.4 dBm (every $P_g = 30$ dBm)

Side lobe level -13.7 dB (2.7 dBi)



Dolph-Chebyshev tapering

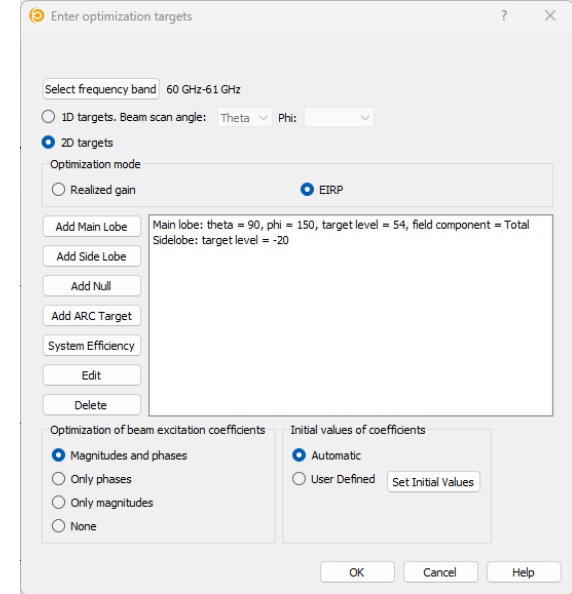
Max gain 15.3 dBi

Max EIRP **53.1 dBm** (max $P_g = 30$ dBm, **min** $P_g = 17$ dBm)

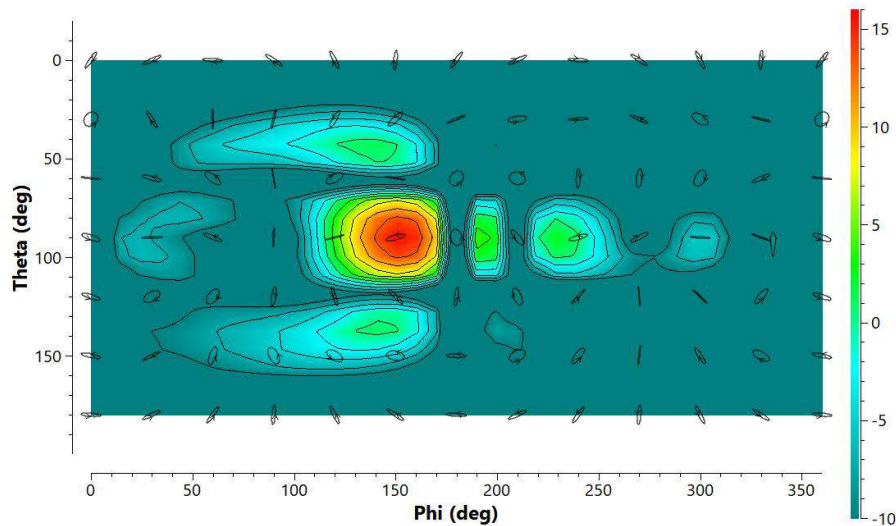
Side lobe level -19.4 dB (-4.2 dBi)

Numerical Beam Optimization in Optenni Lab

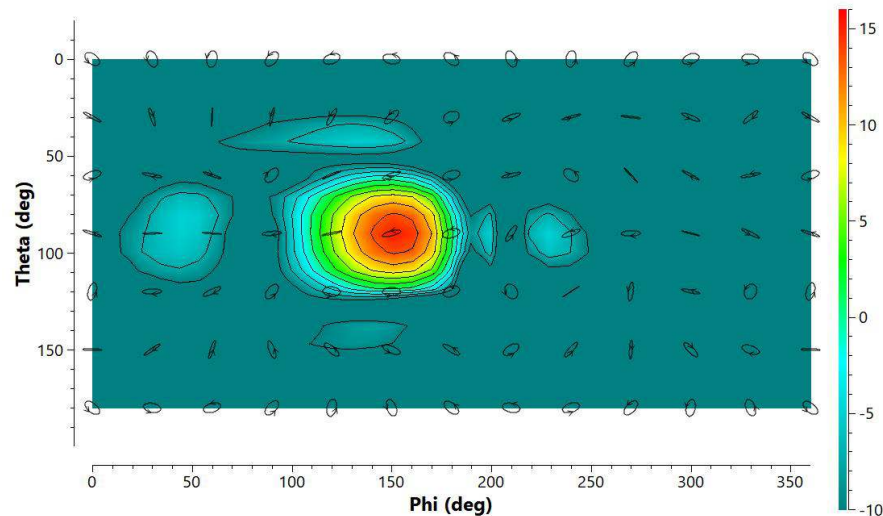
- Numerical beam optimization offers many possibilities of controlling beam properties
 - Main lobe direction and beamwidth
 - Side lobe levels
 - Nulls, polarization
 - Control of active reflection coefficient
 - Control of system efficiency
- The optimizer can vary
 - the magnitudes and phases of the beam,
 - only phases, or
 - only magnitudes
- Optimization can be done for the realized gain or for EIRP
- **Optenni Lab sets you free from the canonical / analytical solutions**



Numerical Optimization Viewed Through Antenna Gain



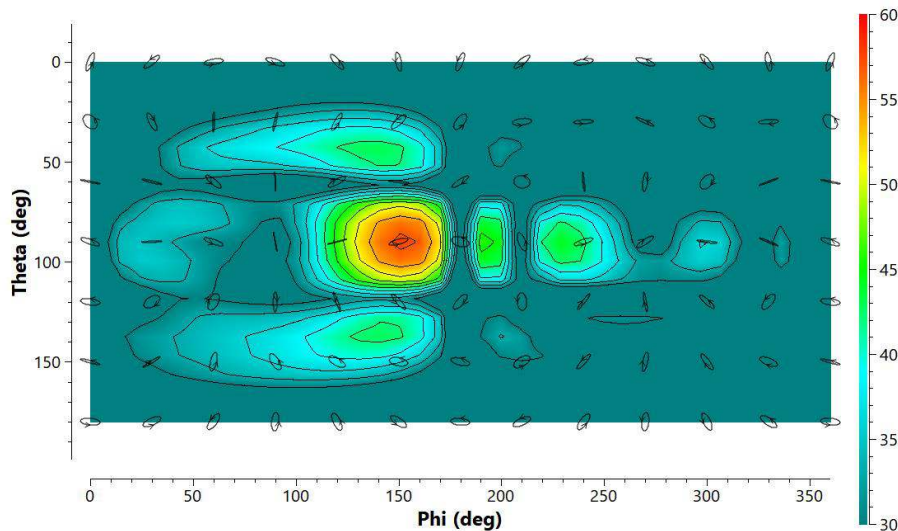
Maximize gain to $\theta=90$, $\phi=150$
→ Realized gain 15.7 dBi ($P_g = 28.8 - 30$ dBm)
→ Side lobe level -11.7 dB (4.0 dBi)



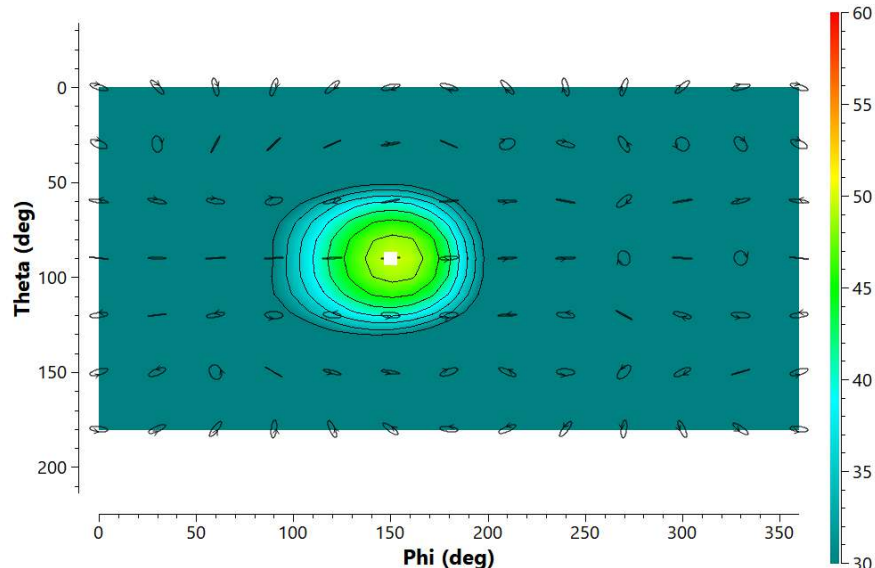
Add a side lobe target to the max.gain target
→ Realized gain 15.2 dBi ($P_g = 21.6 - 30$ dBm)
→ Side lobe level -20.0 dB (-4.8 dBi)

Thus, in terms of gain, main beam drops 0.5dB,
but the sidelobe level can be decreased over 8dB

Numerical Optimization Viewed Through EIRP



Maximize EIRP to $\theta=90$, $\phi=150$
→ EIRP 57.7 dBm (every $P_g = 30$ dBm)
→ Side lobe level -11.8 dB (45.9 dBm)

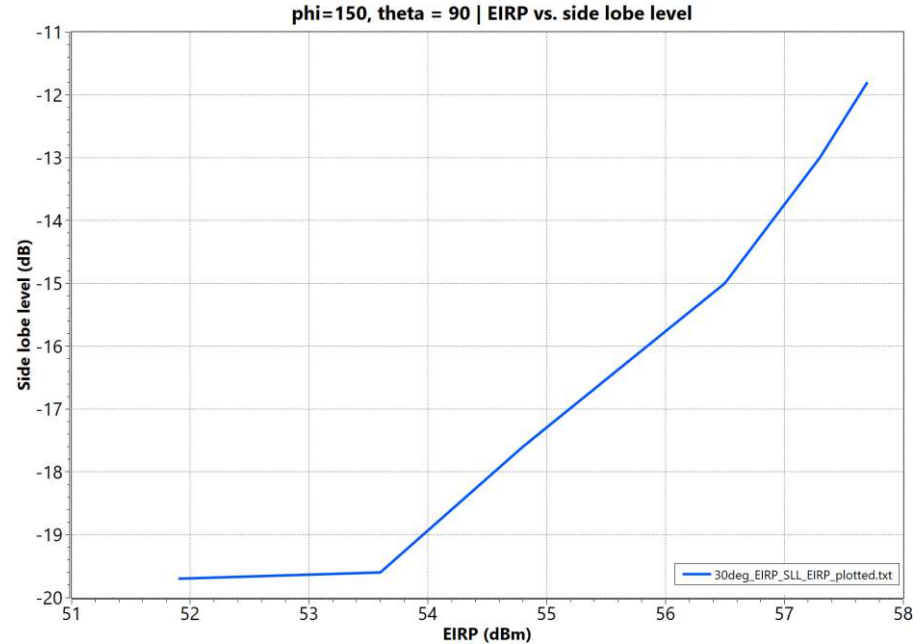


Add a side lobe target to EIRP target
→ EIRP **51.9** dBm ($P_g = 16 - 30$ dBm)
→ Side lobe level -19.7 dB (32.2 dBm)

Thus, in terms of EIRP, main beam drops almost 6dB
when the sidelobe level is decreased approx. 8dB

Engineering EIRP and Side Lobe Level

- By changing the target levels, a sequence of Pareto-optimal compromises between the EIRP and side lobe level can be obtained
- As an example, see graph on the right
- Such graphs are a tremendous help for **engineering** array antennas



Conclusions

- In array beamforming optimization, canonical solutions are fast to compute and lead to good initial guesses for optimization
- Numerical beam optimization enables the control of the main beam properties, side lobe levels, active reflection coefficients and EIRP
- Many of the beam optimization goals are contradictory: e.g. maximization of EIRP and minimization of side lobe levels
- By varying the weights of the optimization criteria, various compromises between the contradictory goals can be obtained
- Optenni Lab lets you take complete control of the array feeding and matching challenge
- Turn messy guesswork of array design into engineering with Optenni Lab

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